



Pemrograman Komputer

oleh

Djoko Luknanto

Departemen Teknik Sipil dan Lingkungan
Fakultas Teknik Universitas Gadjah Mada

Evaluasi Polinomial

Bentuk umum

$$p_n(x) = \sum_{i=0}^n a_i x^i = a_0 + a_1 x + a_2 x^2 + \dots + a_n x^n$$

Contoh:

$$p_n(2) = \sum_{i=0}^n a_i 2^i = a_0 + a_1 2 + a_2 2^2 + \dots + a_n 2^n$$

$$p_2(x) = 6 + 5x + x^2$$

$$p_2(2) = 6 + 5(2) + (2)^2 = 6 + 10 + 4 = 20$$

Secara numeris evaluasi di atas tidak efisien!

Evaluasi Polinomial Efisien

Bentuk umum

$$p_n(x) = \sum_{i=0}^n a_i x^i = a_0 + a_1 x + a_2 x^2 + \dots + a_n x^n$$

diubah menjadi (cara Horner):

$$p_n(x) = a_0 + x(a_1 + x(a_2 + \dots + x(a_{n-1} + a_n x) \dots))$$

terdapat pola berulang $a_n x + a_{n-1}$

bentuk akhir menjadi:

$$p_n(x) = (((\dots(a_n x + a_{n-1})x + a_{n-2})x + \dots + a_1)x + a_0$$

Evaluasi Polinomial Efisien

Contoh $n = 4$

$$p_4(x) = (((a_4 x + a_3) x + a_2) x + a_1) x + a_0$$

Dalam pemrograman bentuk umum

$$p_n(x) = (((\dots(a_n x + a_{n-1}) x + a_{n-2}) x + \dots + a_1) x + a_0$$

$$p_n = (((a_n x + a_{n-1}) x + a_{n-2}) x + \dots) x + a_0$$

algoritmanya menjadi:

1. $P = A(n)$ Algoritmanya sangat sederhana dan langsung

2. For $i = n-1$ to 0

$$P = P * X + A(i)$$

Next i

Evaluasi Polinomial Cara Biasa

Indeks polinomial disesuaikan

$$p_n(x) = \sum_{i=0}^n a_i x^i = \sum_{j=1}^m a_j x^{j-1} = a_1 + a_2 x + a_3 x^2 + \dots + a_m x^{m-1}$$

```
Function Polinomial(X As Single, A As Range) As Double
```

```
' Evaluasi polinomial dengan cara biasa
```

```
Dim j As Integer, Hasil As Double
```

```
Hasil = A(1, 1)
```

perkalian

```
For j = 2 To A.Count
```

perpangkatan

```
    Hasil = Hasil + A(1, j) * X ^ (j - 1)
```

```
Next j
```

```
Polinomial = Hasil
```

penambahan

```
End Function
```

Evaluasi Polinomial Cara Horner

Bentuk akhir cara Horner

$$p_m(x) = (((\dots(a_m x + a_{m-1})x + a_{m-2})x + \dots + a_2)x + a_1$$

```
Function PoliHorner(X As Single, A As Range) As Double  
    ' Evaluasi polinomial dengan cara  
    Dim i As Integer, Hasil As Double  
  
    Hasil = A(1, A.Count)  
    For i = A.Count - 1 To 1 Step -1  
        Hasil = Hasil * X + A(1, i)  
    Next i  
    PoliHorner = Hasil  
End Function
```

Indeks dalam Range artinya A(baris, kolom)

tanpa perpangkatan

penambahan

perkalian

VBA-Excel: Cara Evaluasi Polinomial

X sebagai input pertama

Koefisien polynomial Range (\$B\$3:\$K\$3) sebagai input kedua

Menggunakan Macro

The screenshot shows an Excel spreadsheet titled "Persamaan Polinomial". The first row contains coefficients α_i from 0 to 9. The second row contains powers x^i from 0 to 9. The third row shows the polynomial formula: $Pers: 6,57 + 2,35X - 7,8X^2 + 4,56X^3 - 7,8X^4 + 1,09X^5 - 0X^6 + 0,5X^7 + 0,78X^8 - 1,2X^9$. The fourth row shows the macro formula: `=\B3+\C3*A8+\D3*A8+\D2+\E3*A8+\E2+\F3*A8+\F2+\G3*A8+\G2+\H3*A8+\H2+\I3*A8+\I2+\J3*A8+\J2+\K3*A8+\K2`.

X	Macro	Polinomial
0,500	5,9161718750000	5,9161718750000
1,600	-66,1896959744000	-66,1897035394164
2,700	-6,637,0623509826000	-6,637,0634421613300
-2,300	2,217,9569678974000	2,217,9565186524200
1,760	-141,5071308248280	-141,5071244885550

Cara Biasa (Method 2):

```
Function Polinomial(X As Single, Grup As Range) As Double
    Dim j As Integer, Hasil As Double
    Hasil = Grup(1, 1)
    For j = 2 To Grup.Count
        Hasil = Hasil + Grup(1, j) * X ^ (j - 1)
    Next j
    Polinomial = Hasil
End Function
```

Cara Horner (Method 3):

```
Function PoliHorner(X As Single, Data As Range) As Double
    Dim i As Integer, Hasil As Double
    Hasil = Data(1, Data.Count)
    For i = Data.Count - 1 To 1 Step -1
        Hasil = Hasil * X + Data(1, i)
    Next i
    PoliHorner = Hasil
End Function
```

Hasil hitungan Cara Biasa dan Cara Horner identik, namun dari sisi efisiensi Cara Horner lebih bagus!

Syntax: For...Next Loop

```
For counter = start To end [ Step step ]  
[ statements ]  
[ Exit For ]  
[ statements ]  
Next [ counter ]
```

Perhatikan konvensi
penulisan dalam
manual Bahasa
Pemrograman VBA

Penjelasan dalam [...] boleh tidak ada!

The **For...Next** statement syntax has these parts:

Part	Description
<i>counter</i>	Required. Numeric <u>variable</u> used as a loop counter. The variable can't be a <u>Boolean</u> or an <u>array</u> element.
<i>start</i>	Required. Initial value of <i>counter</i> .
<i>end</i>	Required. Final value of <i>counter</i> .
<i>step</i>	Optional. Amount <i>counter</i> is changed each time through the loop. If not specified, <i>step</i> defaults to one.
<i>statements</i>	Optional. One or more statements between For and Next that are executed the specified number of times.

oleh

Djoko Luknanto

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MENGGUNAKAN VBA- EXCEL INDEX UNTUK AKSES VARIABEL RANGE

Index pada variable Range A(\$C\$4:\$L\$13)

Index A(1,1) selalu mengacu kepada sel pertama dari Range, dalam hal ini \$C\$4

Jumlah baris (i) harus dihitung sebelumnya

Jumlah kolom (j) harus dihitung sebelumnya

		Data berupa Range, A(\$C\$4:\$L\$13)									
		Kolom (j)									
		1	2	3	4	5	6	7	8	9	10
Baris (i)	1	-4.930,636	8.252,820	7.403,666	-1.775,592	-5.737,632	-7.039,365	-1.131,156	8.7449	-871,008	-986,999
	2	-1.014,508	-6.702,628,196	-2.032,442	-372,007	3.034,318	-7.735,076	9.77,633	1.424,572	5.713,734	
	3	2.963,003	3.586,200	-7.160,540	-3.969,212	-6.748,008	2.609,882	5.555,378	7.80,102	7.606,991	-6.429,423
	4	5.813,748	-5.681,320	8.122,424	9.511,659	-8.377,821	-925,260	3.391,837	-495,122	-6.002,378	-6.552,144
	5	-	-	-	-	-	-	-	-	-	-
	6	-	-	-	-	-	-	-	-	-	-
	7	-9.16,826	-2.336,120	1.233,472	-8.188,886	-5.287,350	4.346,124	-2.361,058	2.258,152	414,782	-2.966,683
	8	-7.797,252	-8.173,140	-4.177,985	8.135,578	5.866,760	7.829,143	-2.536,848	1.650,543	-9.543,474	-4.052,065
	9	-2.939,039	-82,333,631	3.066,252	-530,397	-2.917,819	4.794,815	9.632,193	9.379,944	4.477,936	
	10	6.393,997	-7.326,150	3.563,999	-1.118,547	-9.775,967	9.657,431	5.874,609	7.764,309	-993,313	9.413,132

Dalam menggunakan index untuk Range, perlu diperhatikan: (1) Sel pertama yang diacu, (2) jumlah baris dan kolom. Di luar Kawasan Range masih dapat diacu, namun nilainya berisi “sampah” yang mungkin tidak mempunyai arti.

Index pada variable Range Nilai(\$C\$4:\$L\$13)

Jumlah kolom (j) harus dihitung sebelumnya

Index $\text{Nilai}(1,1)$ selalu mengacu kepada sel pertama dari Range, dalam hal ini \$C\$4

The screenshot shows four tables in an Excel spreadsheet:

- Data berupa Range A(\$C\$4:\$L\$13)**: A 10x10 range starting at C4. A green box highlights \$C\$4. A yellow arrow points from the text "Jumlah kolom (j) harus dihitung sebelumnya" to the range.
- Akses dengan index: Nilai(1; j; \$C\$4:\$L\$13)**: A 10x10 range starting at L\$13. A green box highlights L\$13. A green arrow points from the text "Index Nilai (1,1) selalu mengacu kepada sel pertama dari Range, dalam hal ini \$C\$4" to the range.
- Akses dengan index: Nilai(i; i; \$H\$5:\$L\$13)**: A 10x6 range starting at H5. A red box highlights the row index i. A red arrow points from the text "Jumlah baris (i) harus dihitung sebelumnya" to the range.
- Akses dengan index: Nilai(i; j; \$E\$4:\$E\$13)**: A 10x10 range starting at E4. A green box highlights E4.

The tables contain numerical data corresponding to the ranges defined above them.

Dalam menggunakan index untuk Range, perlu diperhatikan: (1) Sel pertama yang diacu, (2) jumlah baris dan kolom. Di luar Kawasan Range masih dapat diacu, namun nilainya berisi “sampah” yang mungkin tidak mempunyai arti.

Index pada variable Range Nilai(\$H\$8:\$L\$13)

Index *Nilai* (1,1) selalu mengacu kepada sel pertama dari Range, dalam hal ini \$H\$8

Jumlah baris (*i*) harus dihitung sebelumnya

Data berupa Range, A(\$C\$4:\$L\$13)									
Kolom (j)									
Baris (i)	1	2	3	4	5	8	9	10	
4	10,294	-9,936,302	-2,798,207	1,502,200	5,836,308	450,663	156,002		
5	36,244	-9,749,009	-8,991,200	-7,819,4	-517,533	-1,428,139	-6,337		
6	147,328	-2,235,159	-9,848,293	2,742,9	-6,697,192	-7,475,933	5,1883		
7	809,335	5,831,059	3,784,675	-3,055,520	2,144,491	-2,936,171	9,766,271	-9,064,296	
8	718,849	-3,703,593	-9,564,509	-745,271	-980,928	-5,935,806	3,979,301	-378,816	-3,099,424
9	5,930,858	4,438,945	-452,969	-7,000,044	-7,231,060	5,968,502	-3,772,188	73,188	-4,683,335
10	7,156,727	4,057,548	1,235,544	-7,052,038	2,384,819	-2,682,841	-9,186,269	82,395	-2,492,721
11	4,713,794	2,693,279	9,970,836	2,779,980	1,01,224	5,044,000	7,239,412	76,558	5,702,20
12	-8,330,567	7,830,607	543,924	-5,539,043					
13	7,072,704	-6,575,435	8,393,848	9,262,852	-693,054	2,857,921	-9,447,708	-103,713	-1,871,161
14									

Akses dengan index: NilaiSel (i; j; \$C\$4:\$L\$13)										
Kolom (j)										
Baris (i)	1	2	3	4	5	6	7	8	9	10
1	-980,928	-5,935,806	3,979,301	5,235,816	-3,099,424	0,000	0,000	5,000	-7,615,241	-3,718,849
2	-7,231,060	5,968,502	-3,772,188	3,873,188	-4,683,335	0,000	0,000	6,000	-4,294,663	-8,930,858
3	2,384,819	-2,682,841	-9,186,269	2,882,395	-2,492,721	0,000	0,000	7,000	-4,603,915	-5,156,727
4	1,291,234	5,944,900	7,328,412	-3,276,558	-5,793,310	0,000	0,000	8,000	-7,937,990	-4,713,794
5	-8,648,296	216,667	7,216,175	7,650,624	1,748,898	0,000	0,000	9,000	-240,348	-8,330,567
6	-693,054	2,857,921	-9,447,708	6,013,713	-1,871,006	0,000	0,000	10,000	-6,649,897	7,072,704
7	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000
8	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000
9	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000
10	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000

Akses dengan index: NilaiSel (i; j; \$H\$8:\$L\$13)										
Kolom (j)										
Baris (i)	1	2	3	4	5	6	7	8	9	10
1	5,836,308	450,663	156,002	0,000	Baris (i)	1,000	9,032,315	7,710,294	-9,936,302	-2,798,207
2	-517,533	-1,428,139	-6,337	0,000		2,000	-3,697,412	236,244	-9,749,009	-8,991,200
3	6,503,103	2,447,328	-2,235,159	0,000		3,000	6,503,103	2,447,328	-2,235,159	-9,848,293
4	5,840,794	8,809,335	5,831,059	3,784,675	-3,055,520	4,000	7,430,851	-2,936,171	2,144,491	-9,766,274
5	-7,615,241	-3,718,849	-3,703,593	9,564,509	-745,271	5,000	-9,809,282	-5,935,803	3,979,301	5,235,816
6	-4,294,663	-8,930,858	4,438,945	-452,969	-7,000,044	6,000	5,968,502	-3,772,188	3,873,188	-4,683,335
7	-9,737,990	-4,713,794	-2,693,279	9,970,836	2,779,980	8,000	1,291,234	-5,944,900	-7,328,412	-3,276,558
8	-240,348	-8,330,567	7,830,607	543,924	-5,539,043	8,648,296	216,667	7,216,175	7,650,624	1,748,898
9	-6,649,897	7,072,704	-6,575,435	8,393,848	9,262,852	-693,054	2,857,921	-9,447,708	-6,013,713	-1,871,006
10	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000

Akses dengan index: NilaiSel (i; j; \$J\$4:\$J\$13)										
Kolom (j)										
Baris (i)	1	2	3	4	5	6	7	8	9	10
1	5,836,308	450,663	156,002	0,000	Baris (i)	1,000	9,032,315	7,710,294	-9,936,302	-2,798,207
2	-517,533	-1,428,139	-6,337	0,000		2,000	-3,697,412	236,244	-9,749,009	-8,991,200
3	6,503,103	2,447,328	-2,235,159	0,000		3,000	6,503,103	2,447,328	-2,235,159	-9,848,293
4	5,840,794	8,809,335	5,831,059	3,784,675	-3,055,520	4,000	7,430,851	-2,936,171	2,144,491	-9,766,274
5	-5,391,867	-2,186,269	-2,091,234	7,000	-6,649,897	7,072,704	0,000	0,000	0,000	0,000
6	-6,292,721	-2,492,721	0,000	0,000	0,000	0,000	7,000	-4,603,915	-5,156,727	4,057,548
7	-9,186,269	-2,693,279	-2,603,310	0,000	0,000	0,000	8,000	-7,937,990	-4,713,794	-2,693,279
8	-7,328,412	-2,898,412	-2,803,315	0,000	0,000	0,000	9,000	-240,348	-8,330,567	7,830,607
9	-7,216,175	-2,988,175	-2,998,398	0,000	0,000	0,000	9,000	-240,348	-8,330,567	543,924
10	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000	0,000

Hasil yang valid hanya dalam kawasan ini (sesuai ukuran data), yang lainnya sampah!

Jumlah kolom (*j*) harus dihitung sebelumnya

Index pada variable Range Nilai(\$E\$4:\$L\$13)

Jumlah baris (*i*)
harus dihitung
sebelumnya

Index *Nilai* (1,1) selalu mengacu
kepada sel pertama dari Range,
dalam hal ini \$E\$4

Daftar Perkiraan Range, A(\$C\$4:\$L\$13)

		Kolom (j)									
		4	5	6	7	8	9	10			
Baris (i)	1	-3.002.074	-4.190.644	6.321.821	4.382.521	4.493.650	3.526.834	4.916.852	-5.173.179	7.263.431	-8.993.830
	2	-5.370.499	-8.697.036	4.035.901	4.085.572	0,971	-3.635.526	-7.584.319	2.465.510	-9.010.549	6.260.559
	3	-7.297.024	-6.233.583	3.113.394	9.488.879	3.049.302	4.496.868	3.837.515	4.812.433	-3.963.116	6.513.767
	4	6.889.654	-6.330.674	9.211.961	7.884.185	-3.944.513	-408.361	-108.221	2.331.434	278.845	4.225.929
	5	886.016	8.850.712		6.131.085	9.478.909	5.569.710	-6.596.026	6.393.511	-5.053.901	-4.802.864
	6	8.566.012	1.319.916		8.594.143	5.171.779	-7.538.073	-2.145.957	8.453.633	-2.651.646	7.717.521
	7	-131.502	-8.097.675	-4.198	3.387.691	4.655.061	1.622.945	5.339.291	8.773.865	-3.663.421	-4.887.684
	8	-9.179.248	-571.115	-1.536	2.538.843	-1.053.564	-1.137.874	-9.075.287	2.072.065	-2.174.751	-3.466.675
	9	3.262.993	-1.732.103	-1.653	8.982.757	-690.760	7.458.535	7.335.957	4.157.558	9.701.575	3.034.676
	10	3.594.628	-9.538.305	-2.215	3.341.643	5.198.087	-1.121.691	884.057	-144.487	-6.869.577	-5.548.750

Akses dengan index: Nilai (i; j; \$H\$5:\$L\$13)

		Kolom (j)									
		3	4	5	6	7	8	9	10		
Baris (i)	1	5.569.710	-6.596.026	6.393.511	-5.053.901	-4.802.864	0,000	0,000	5,000	886.016	8.850.712
	2	-7.538.073	-2.145.957	8.453.633	-2.651.646	7.717.521					
	3	1.622.945	5.339.291								
	4	-1.137.874	-9.075.287	-4.198	3.387.691	4.655.061	1.622.945	5.339.291	-1.137.874	-9.075.287	2.072.065
	5	7.458.535	7.335.957	-1.536	2.538.843	-1.053.564	-1.137.874	-9.075.287	2.072.065	-2.174.751	-3.466.675
	6	-1.121.691	8.982.757	-690.760	7.458.535	7.335.957	4.157.558	9.701.575	3.034.676		
	7	0,000			0,000	0,000	10.000	3.594.628	9.538.305		
	8	0,000			0,000	0,000	0,000	0,000	0,000		
	9	0,000			0,000	0,000	0,000	0,000	0,000		
	10	0,000			0,000	0,000	0,000	0,000	0,000		

Jumlah kolom (j)
harus dihitung
sebelumnya

Hasil yang valid hanya dalam
kawasan ini (sesuai ukuran data),
yang lainnya sampah!

oleh

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BEBERAPA JENIS VBA- EXCEL DO LOOP

Do...Loop statement (1/2)

Syntax

- **Do [{ While | Until } condition]**
[statements]
[Exit Do]
[statements]
Loop
- 
- While | Until di depan**

Or, you can use this syntax:

- **Do**
[statements]
[Exit Do]
[statements]
Loop [{ While | Until } condition]
- 
- While | Until di belakang**

Do...Loop statement (2/2)

While | Until di depan

```
Public Sub LoopExample()
    Dim Check As Boolean, Counter As Long, Total As Long
    Check = True: Counter = 0: Total = 0 ' Initialize variables.
    Do ' Outer loop
        Do While Counter < 20 ' Inner Loop
            Counter = Counter + 1 ' Increment Counter.
            If Counter Mod 10 = 0 Then ' Check in with the user on every multiple of 10.
                Check = (MsgBox("Keep going?", vbYesNo) = vbYes) ' Stop when user click's on No
                If Not Check Then Exit Do ' Exit inner loop.
            End If
        Loop
        Total = Total + Counter ' Exit Do Lands here.
        Counter = 0
    Loop Until Check = False ' Exit outer loop immediately.
    MsgBox "Counted to: " & Total
End Sub
```

While | Until di belakang